



# Escher and the Endless Staircase

NAME: .....

CLASS: .....

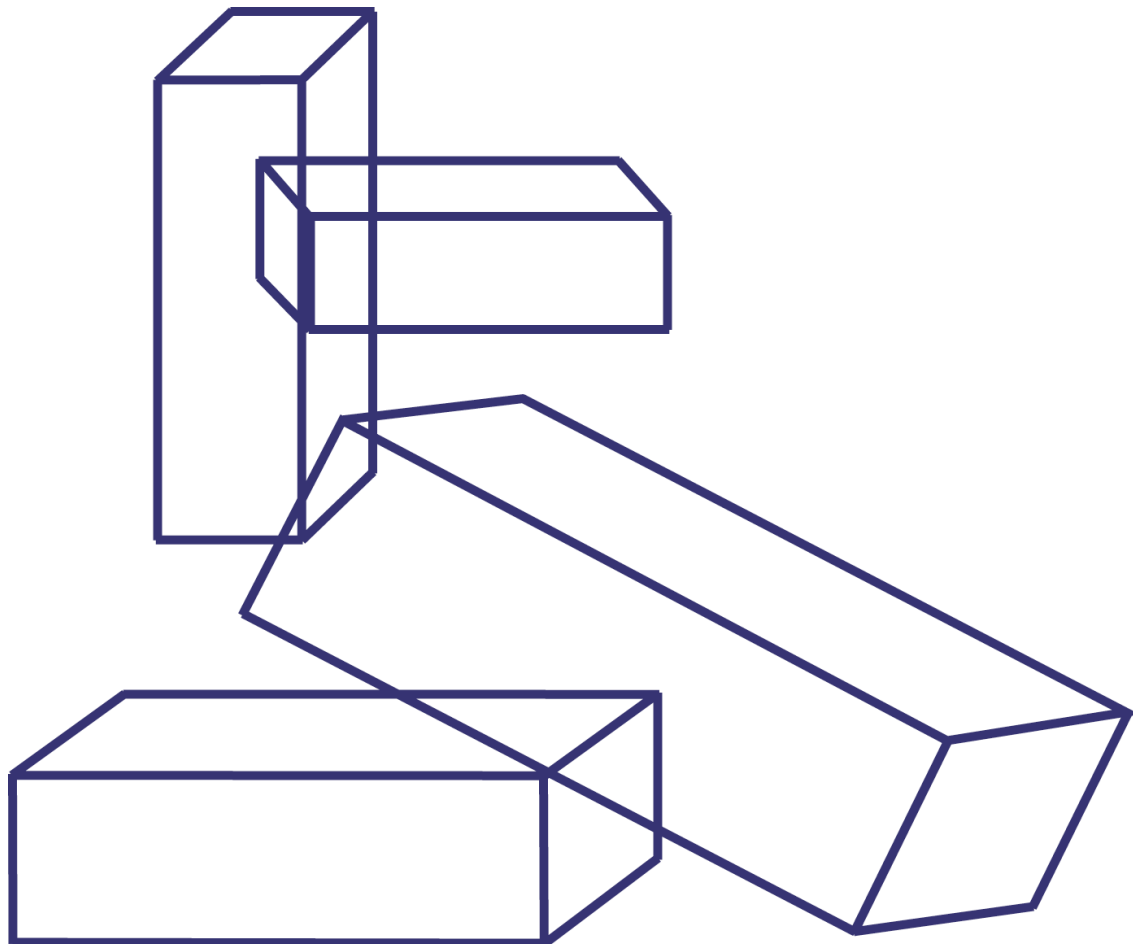
DATE: .....



## Basic/Core

Below are four cuboids that have been drawn without a sense of depth, i.e. there is no indication of which cuboid is at the front or which is at the back of the drawing. Using tracing paper, create a sense of depth by following the instructions below.

- 1) Trace over the cuboid you wish to be at the front of the drawing.
- 2) Next, trace over the cuboid you wish to be directly behind the first cuboid. Do not trace any parts which overlap the first cuboid.
- 3) Repeat this process with the remaining two cuboids.





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## Advanced

### Proof By Contradiction (for discussion)

1) One way to show that a statement is true is to first assume that it is false, then to look for an implication of it being false which leads to a contradiction, and thus conclude that the original statement is true. In this way prove that:

a) a triangle can only have one right angle.

b) a polygon must have at least three sides.

c) at most a triangle only has one right angle.

d) an octagon has eight sides.

e) all the angles in an equilateral triangle are  $60^\circ$ .

2) For these complex numbers, calculate the following:

a)  $i + 5i$

b)  $2 + 4 + 6i$

c)  $2i + i$

d)  $-8i - 7i$

e)  $-1 - 8i - 4 - i$

f)  $7 + i + 4 + 4i$

g)  $4i(-2 - 8i)$

h)  $(7 - 6i)(-8 + 3i)$



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## ANSWERS

### Advanced

2) a)  $6i$

b)  $6+6i$

c)  $3i$

d)  $-15i$

e)  $-5-9i$

f)  $11+5i$

g)  $-8i+32$

h)  $-38+69i$